



36 and pipes of negligible length (i.e., negligible pressure loss), to assess the supplying
37 capability of a network under pressure deficient conditions using demand driven simulation
38 software. This paper illustrates a simple way to assess the supplying capacity of demand
39 nodes under pressure deficient conditions by assigning the respective emitter co-efficient
40 only to those nodes facing pressure deficit condition. The proposed method is tested with
41 three bench-mark networks and it is able to simulate the network without addition of any
42 fictitious network elements or changing the source code of the software like EPANET.

43 **Keywords:** Water distribution network, Demand-driven analysis, Pressure-driven analysis,
44 Emitter, Fire demand.

45

46 **1.0 Introduction**

47 Analysis of water distribution systems under pressure-deficient conditions presents a
48 challenging research area as understanding and simulating the real scenario is complex. It is
49 well known that DDA simultaneously solves the mass balance and energy balance equations
50 to determine the flow in each pipe for a given network topology and configuration. However,
51 such DDA solution does not represent an exact behaviour of the system when it is under
52 pressure-deficient conditions or if a bound on service pressure is assigned. It is possible to
53 notice the negative pressure in DDA whenever the total loss of head occurring from source to
54 node exceeds available source head. This mainly happens when the demand assigned to a
55 node is higher than what the pipes incident to that node actually can carry based on the
56 available source head. To compute the actual outflows from the nodes within given pressure
57 bounds, modifications are needed either in the source code of demand driven simulation
58 engine (e.g., Cheung et al. 2005) or by adding additional fictitious components like
59 reservoirs, check valves, flow control valves, emitters, dummy nodes and very short pipes to
60 the demand nodes (e.g., Ozger 2003; Ang and Jowitt 2006; Rossman 2007; Suribabu and
61 Neelakantan 2011; Jinesh babu and Mohan 2012; Gorev and Kodzheshpurova 2013;



62 Sivakumar and Prasad 2014; Morley and Tricarico 2014; Abdy Sayyed et al. 2014 and 2015;
63 Sivakumar and Prasad 2015; Suribabu 2015; Mamizadeh and Sharoonizadeh 2016; Suribabu
64 et al. 2017; Mohmoud et al. 2017; Pacchin et al.2017).

65 Mohmoud et al. (2017) addressed the shortcoming of each of these methods for
66 evaluating outflow in the case of large networks and under extended period simulation
67 (EPS).They have developed a new way to handle PDA using EPANET in single iterative type
68 after an introduction of a check valve, a flow control valve and a flow emitter for both steady
69 state and EPS.

70 **2.0 Pressure Driven Analysis-Literature Review**

71 In the beginning, pressure-deficient condition was considered as a rare phenomenon and/or a
72 typical problem in operational scenario. However, when concern on reliability gained
73 importance, the failure scenarios were analysed and thus analysis of pressure-deficient
74 conditions became popular. Two approaches are popular for analyzing pressure deficient
75 condition. In the first approach a specific pressure-demand relationship is embedded in the
76 source code of the simulator (requires changing of source code). Some of the important
77 studies using this approach by several authors are presented in tabular form below (Table 1).

78

79 Apart from the above tabled researches, Liu et al. (2011), and Siew and Tanyimboh (2012)
80 adopted different methodologies to obtain node heads in EPANET. Giustolisi et al. (2011)
81 developed and used new Excel based software called WNetXL. Generally, the limitations
82 of this approach (Mahmoud et al. 2017) are: (1) they require a change in algorithm and
83 program code, (2) the computer codes are not available, (3) requires iterations, (4) most of
84 them demonstrated on sample networks, and (5) they exhibit difficulty in handling extended
85 period simulation.



86

87 Some of the researchers in the recent years attempted pressure deficient analysis using
88 EPANET (popular freeware demand driven model) by introduction of a few artificial or
89 imaginary components like reservoir, flow control valve, check valve, emitter, but without
90 node head-flow relationships. These researches claim less number of iterations and the recent
91 researches claim single iteration (no iteration). The works using components in demand
92 driven model for pressure deficient analysis are presented in Table 2.

93

94 Literature review indicates that the approach of using demand-driven engine to get the
95 pressure-driven results is getting more attention. It is due to computational convenience and
96 promising trend of development. Hence, this research is also planned to focus on this
97 approach. This paper proposes a simple approach to suit both single period and EPS but
98 without addition, deletion, opening and closing of network elements. Proposed method
99 requires only assigning emitter co-efficient and altering nodal elevation by incorporating
100 minimum pressure head with existing elevation. Though the method is an iterative type, it
101 can be easily implemented irrespective of the size of network.

102

103 **3.0 Background of Emitter based approaches**

104

105 EPANET 2 (Rossman 2000) hydraulic simulation engine contains a special element called
106 Emitter that behaves as a sprinkler head at the node and delivers an outflow proportional to
107 available pressure head. Rossman (2007) discussed the possibility of building the pressure
108 driven network analysis (PDNA) proposed by Ang and Jowitt (2006) in EPANET hydraulic
109 solver using this emitter feature. Further, Suribabu (2015) proposed a method to use emitter
110 as a replacement to the connection of fictitious reservoirs to all the demand nodes (DNs).



111 Here, the emitter determines the possible supply at all deficient nodes based on its available
 112 pressure head. The flow from the emitter is expressed as follows (Rossman 2000):

$$113 \quad Q = K_e p^n \quad 1$$

114 Where Q is nodal outflow, K_e is the emitter co-efficient, n is the emitter exponent and p is
 115 pressure. Rossman (2007) suggested that the value of emitter co-efficient can be calculated
 116 according to the properties of the pipe that connects the node and the artificial reservoir (i.e.,
 117 diameter, length and Hazen-William co-efficient), in order to make it equivalent to the
 118 approach of Ang and Jowitt (2006). Another emitter based approach was proposed by Abdy
 119 Sayyed et al. (2015) which is a non-iterative method by connecting a check valve (CV), a
 120 flow control valve (FCV) and an emitter to the demand nodes. Further, they have shown that
 121 emitter equation is identical with Wagner (1988) for $H_j^{req} \geq H_j^{min}$, if emitter co-efficient K_e
 122 and exponent γ are taken as follows:

$$123 \quad K_e = \frac{Q_j^{req}}{(H_j^{req} - H_j^{min})^\gamma} \quad 2$$

$$124 \quad \gamma = \frac{1}{n_j} \quad 3$$

125 Where the nodal elevation of the emitter set nodes should be:

$$126 \quad NEL_j = EL_j + H_{min} \quad 4$$

127 Rossman (2000) also suggested that to get maximum flow at minimum pressure at demand
 128 nodes, the emitter co-efficient shall be assigned as 100 times of the respective nodal demand.
 129 Hereafter it is referred as K_{e100} (Co-efficient of discharge).

$$130 \quad K_{e100} = 100 \times Q_j^{req} \quad 5$$

131 In Abdy Sayyed et al. (2015), the FCV is used to fulfil the maximum flow constraint and the
 132 CV is employed to avoid flow reversal. Single iteration pressure driven analysis (SIPDA)
 133 proposed by Mohmoud et al. (2017) adopted the same sequence of network elements as that



134 of Abdy Sayyed et al. (2015) approach. But, SIPDA adds the sequence of network elements
 135 and modifies their nodal elevations only to those nodes experiencing pressure-deficit.
 136 Pacchin et al. (2017) used another new sequence of elements (General Purpose Valve (GPV),
 137 Check Valve (CV) and artificial Reservoir) to evaluate outflow from the node under pressure-
 138 deficient conditions. Pacchin et al. (2017) applied the proposed approach and other similar
 139 methods to two real water distribution networks and concluded that their proposed method
 140 and Abdy Sayyed et al. (2015) are able to produce correct the behaviour of the network under
 141 pressure deficient condition. However, the drawback of these methodologies is the need to
 142 include two dummy nodes per node which further increases the number of components and
 143 the topology complexity of the network. Though addition of elements make single snapsort
 144 analysis, its incorporation to each demand nodes make network too complex in topology. It
 145 consumes lot of time of the network modeller unless separate integrated component is created
 146 with setting option in the existing software.

147

148 **4.0 Assumptions**

149 Many investigators (Bhave 1981; Germanopoulos 1985; Wagner et al. 1988; Reddy and
 150 Elango 1989, 1991; Chandapillai 1991; Fujiwara and Ganesharajah 1993; Tucciarelli et al.
 151 1999; Tanyimboh et al. 2001; Wu et al. 2009; Tanyimboh and Templeman 2010) have
 152 suggested different head-flow relations for assessing the supplying capability of nodes under
 153 pressure-deficient conditions. Figure 1, presents an interpretation of the head-flow relations.

154 Given the variables defined in Figure 1, there are different assumptions that the modeller can
 155 make:

- 156 - The more general case is the one in which no assumption is made on Z , H_{min} , H_{req} .

157 In this case the minimum possible head on a node is its elevation Z , and if hydraulic



158 conditions do not permit, then the node is isolated representing not only that demand
 159 in the node must be zero, but also that there is no flow in the adjacent pipes (i.e. no-
 160 siphonic flow is considered). If the head is between Z and H_{min} , then the demand at
 161 the node is still zero, but now flow in the adjacent pipes can happen if hydraulic
 162 conditions downstream permit it. If the head is between H_{min} and H_{req} , then the
 163 demand at the node is only partially fulfilled even though the appliance(s) are
 164 completely open; this is modelled with a transition curve which can take different
 165 forms (e.g. Germanopoulos 1985; Bhave 1989; Salgado-Castro 1988; Wagner et al.
 166 1988; Fujiwara and Li 1998; Tanyomboh and Templeman 2010) although
 167 Germanopoulos (1985) emitter equation is commonly accepted as the most
 168 physically appropriate. If the head is above H_{req} , then the pressure in the appliance is
 169 enough to fulfil the required demand and therefore the appliances are assumed be
 170 partially closed to receive only the required demand; this means that a demand driven
 171 analysis of the node is suitable.

- 172 - Assume $Z < H$ (assume the actual junction elevation is below any possible value of
 173 H). This case assumes that the water cannot ever reach the Node Isolation Zone.
 174 Models that accept negative pressures in the system and flows downstream on these
 175 nodes are either making this assumption, or assuming syphonic flow conditions (as
 176 long as the absolute pressure is above vapour pressure).
- 177 - Take $H_{min} = Z$. This case assumes that once there is some pressure in the node, there
 178 is some outflow. This assumption is valid when the node elevation actually represents
 179 the elevation of the lowest water demand appliance among all of the appliances
 180 lumped in it.
- 181 - Take $H_{req} = H_{min}$. This case assumes that once the head is above the minimum head
 182 (i.e., pressure in the emitter is above zero) the outflow is equal to the required flow or,



183 failing that, the maximum hydraulically-possible flow. This assumption can be
184 modelled using Rossman (2000) approximation of using a emitter coefficient of
185 $100 \cdot Q_{Req}$.

186 The method proposed in this study requires no assumptions on Z , H_{min} , H_{req} , although it
187 can deal with any of the previously mentioned ones. This means the only assumptions made
188 in the proposed pressure driven analysis (PDA) are as follows:

- 189 1. Though available pressure is greater than required pressure, the outflow at demand
190 nodes does not exceed its design demand. This is a very basic assumption made by
191 municipal engineering at the project formulation stage.
- 192 2. No outflow is possible at demand node if available pressure is less than minimum
193 service pressure.
- 194 3. Pressure dependent outflow between required and minimum pressures takes the form
195 as shown in Fig. 1 and for the corresponding condition the percentage of valve
196 opening is defined by the curve.
- 197 4. Water distribution network is considered as a non-air-tight system. Hence, no
198 siphonic flow is possible in the network.
- 199 5. Emitter co-efficient is considered based on either eq. 2 or 100 times the nodal demand
200 to estimate the outflow at minimum residual pressure (Eq. 5).

201 **5.0 Proposed method**

202 The present study, proposes a simple approach by setting emitter co-efficient and changing
203 the elevation of the nodes that have been identified as pressure-deficient through few
204 simulation runs of DDA. The proposed approach completely eliminates the serial inclusion of
205 fictitious network elements at any node of the system. The entire procedure is illustrated by a
206 flow chart shown in Fig. 2.



207 For a given condition, the network initially should be simulated using EPANET 2, identifying
208 the maximum pressure-deficient node and setting its demand as zero. This process should be
209 implemented repeatedly until all the nodes get $H_{avl} \geq H_{req}$. Now, it is to be noted here that all
210 non-zero nodes could deliver the design demand. Then, increase the elevation of zero-set
211 nodes to H_{min} (ie. $EL_j + H_{min}$) and calculate the emitter co-efficient to be assigned to those
212 nodes. Next, the network is simulated again. If a negative flow takes place at any emitter-set
213 node, then remove the emitter value of those nodes and perform again DDA and interpret the
214 results. Now there are chances of H_{avl} in some nodes going below H_{min} as the coefficient of
215 the emitter with negative flows has been set to zero. Now such nodes cannot behave as
216 sources. Hence, if pressure in some nodes gets less than minimum pressure, then again set the
217 zero demand and change the nodal property as mentioned above and simulate the network.
218 The analysis ends only if no negative flow exists and none of the non-zero demand nodes
219 experience H_{avl} less than H_{min} . At the end of the analysis, if any nodes show negative pressure,
220 then close the pipes incident to those nodes and simulate again to get final solution. The
221 procedure is illustrated further by a flow chart (Fig.2).

222 5.1 Example 1

223 A single-fixed source head two-loop network with six demand nodes and eight links
224 (proposed by Ang and Jowitt (2006) for PDA) is considered to illustrate the proposed
225 approach (see Fig.3). Each pipe is 1000 m long with a Hazen-Williams coefficient of 130.
226 The nodal demand for each node is 25 L/s. DDA shows the full delivery of design demand at
227 respective elevation under normal conditions. To test the proposed algorithm, three scenarios
228 are considered: (i) closing of pipe 3 (ii) Fire demand of 50 L/s at node 2 and (iii) Fire demand
229 of 50 L/s at node 7. Table 3 provides both DDA and proposed PDA results for all three
230 scenarios. Equation 5 is used to simulate the pressure-flow relation (equivalent to a difference



231 between required and minimum pressures below 0.001 m if using eq. 2) with an emitter
232 exponent of 0.54.

233 DDA shows negative pressure at all the demand nodes except node 2 while pipe 3 is isolated
234 from service (Scenario 1). Node 4 is observed as maximum negative pressure node and its
235 nodal demand is set as zero. Again hydraulic simulation is carried out to verify whether all
236 nodes turned into pressure above zero. But, still node 6 is facing higher pressure deficit
237 condition among nodes 3 to 7 and its demand is set as zero. After setting emitter co-efficient
238 to both node 4 and 6, the hydraulic analysis shows a negative flow at node 4 and a negative
239 pressure at node 7. By disconnecting pipes incident to node 4 and removing its K_e the other
240 outflows are computed. This scenario requires five demand driven analyses to obtain PDA
241 results. Further, same result is obtained using SIPDA proposed by Mohmoud et al. (2017)
242 after disconnecting incident pipes to node 4. SIPDA took three DDA run after addition of
243 artificial links between network elements and five nodes.

244 In the next case (scenario 2), a fire demand of 50 L/s is created at node 2. The total demand at
245 node 2 is changed as 75 L/s. As this node is nearer to the source, there is more possibility to
246 satisfy the extra demand. But, DDA analysis indicates negative pressure to all the nodes as
247 the total demand of that node is increased three times the design demand (i.e., two times
248 higher than the existing demand). Nodal demand at node 3 and 7 is modified as zero
249 sequentially after noticing negative pressure. Now, network shows pressure greater than H_{min}
250 at these nodes. Hence, it is possible to deliver partially the flow to those nodes with zero
251 demand set. Now Emitter co-efficient is set both to nodes 3 and 7 and network is simulated.
252 No negative pressure or negative flow is detected at these two nodes. But, pressure at node 5
253 has become negative. By changing nodal demand and setting emitter co-efficient at node 5
254 provided a final result after simulation. It can be seen that network is able to supply full fire
255 demand at node 2, full supply at node 4 and 6, and partial supply at node 3, 5 and 7. SIPDA



256 provided the same result while emitter co-efficient is taken as 2500. Analysis by SIPDA
257 necessitates addition of serial fictitious network elements to all the demand nodes as all the
258 nodes experienced negative pressure upon 50 L/s fire demand at node 2.

259 In the third scenario, a fire demand of 50 L/s at node 7 is added and the network is simulated.
260 Application of proposed approach and SIPDA provided the same results.

261 **5.2 Example 2**

262 The network 1 is used as it is for further analysis by setting reservoir elevation as 135 m
263 instead of 100 m. The minimum and required pressures at all the demand nodes are
264 designated as 15 m and 30 m respectively. DDA analysis indicates that network can supply
265 design demand from all the demand nodes at required pressure level of 30 m. SIPDA and the
266 proposed approach requires Emitter co-efficient, K_e . For demand 25 L/s with $H_{req} = 30$ m and
267 $H_{min} = 15$ m, the emitter co-efficient is obtained as $5.80 \text{ L/s/m}^{0.54}$. The same value is utilised
268 for both approaches to simulate the behaviour of network under link 3 isolation.

269 PDA analysis is carried out by proposed approach. DDA needs to be run five times and
270 results obtained are presented in Table 4. Proposed method indicates full supply of design
271 demand at nodes 2 and 3 while the remaining nodes are able to supply only partial demand.
272 For the same case study, SIPDA makes partial supply at nodes 4, 6 and 7 while recorded
273 pressure is in between H_{min} and H_{req} . Though the pressure at node 5 is below H_{req} , SIPDA
274 indicates the full supply of demand instead of partial supply. SIPDA result at this node
275 violates the assumption of partial supply in between minimum and required pressure.

276 Further, by closing two links 3 and 6, the network is simulated and DDA shows pressure
277 below minimum at nodes 4, 5, 6 and 7. By applying proposed approach, actual demands and
278 pressures are evaluated and presented in Table 4. Under pipes 3 and 6 failure condition,



279 network is able to supply full design demand at nodes 2 and 3. The remaining nodes are able
280 supply partial demand only.

281 **5.3 Example 3**

282 A multisource pumped water distribution network presented by Jinesh babu and Mohan
283 (2012) is considered for further testing of the proposed approach. Fig. 4 shows the network
284 layout consisting of two pumps with capacity of 125 kW each instead of 125 hp considered
285 by Jinesh babu and Mohan (2012) and designed to deliver 2/3rd of total demand. These two
286 pumps, P1 and P2 pump the water from two sources, S1 and S2 respectively whose
287 elevations are 100 m each. The remaining 1/3rd of total demand shall be drawn from
288 reservoir, S3 whose elevation is 200 m and one flow control valve is provided between
289 reservoir S3 and node 7 in order to control the flow to 1/3 of total demand. A demand pattern
290 with four intervals is considered with demand factors (DFs) of 0.2, 1.0, 0.6 and 0.8 which
291 represent time intervals of 0.00 to 6.00, 6.00 to 12.00, 12.00 to 18.00 and 18.00 to 24.00 h
292 respectively. The optimal speed of pumps for respective time interval needs to be set as
293 0.584, 1.0, 0.842 and 0.927. Hazen-Williams roughness co-efficient of 130 is assumed for all
294 the pipes. As Jinesh babu and Mohan (2012) did not specify on upper and lower service
295 pressure limit to the network, it is assumed in the present study that the required and
296 minimum pressure needed for each demand node as 30 m and 15 m respectively. Table 5
297 presents the pipe and nodal properties of the network. Table 6 shows the required nodal
298 outflows at four time steps.

299 Pump 1 failure case is analysed to examine the proposed approach. The results of EPS
300 analysis for four time steps are presented in Table 7. This scenario produces partial flow at
301 several nodes in all time steps. It is to be noted that in first and second time steps, all nodes
302 supply some water whereas in the next two time steps, node 1 is unable to deliver even partial



303 flow. Two nodes at time steps 1 and 2 indicates pressure greater than H_{req} with full supply
304 conditions and all remaining nodes have H_{avl} between H_{min} and H_{req} . While in case of time
305 step 3 and 4 no nodes are noticed with H_{avl} greater than H_{req} . This indicates that the proposed
306 approach is able to simulate the pressure based flow when the network is energized by pumps
307 apart from gravity flow by reservoir. The network is able to supply 71.17 %, 69.34%, 70.99%
308 and 71.37 % of its total design demand at respective time steps. But, it is to be noted here that
309 the drop in supply under failure of component is not uniform to all the nodes. While
310 optimizing the network, the various components of the network should be sized in such a way
311 that, to a possible extent, all nodes get affected uniformly under failure of any component so
312 that equity can be maintained under failure scenarios. To achieve this PDA is becoming very
313 important.

314 **5.4 Example 4**

315 To examine the applicability of proposed approach on a large size benchmark network, a
316 Modena Network (MOD) given by Centre for Water Systems, University of Exeter (Wang et
317 al. 2015) is considered. Its layout is shown in Fig. 5 and it consists of 317pipes, 268 demand
318 nodes, and four reservoirs with fixed head within 72.0 m to 74.5 m. In the present work, the
319 layout, its diameter and Hazen-Williams roughness coefficient of 130 are considered as it is
320 given with the network. The minimum and required pressures are assumed as 10 m and 20 m
321 respectively. Supply from Reservoir ID 272 is stopped fully by isolation of a pipe connecting
322 reservoir and nearest node. DDA indicates pressure deficit (i.e., below H_{req}) in 171 demand
323 nodes. Using EPANET Toolkit, the proposed approach is implemented and the results are
324 presented in Fig.6. Actual outflow versus design demand plot (Fig.6) shows the number of
325 full supply and partial supply nodes. The trajectory of points lying along diagonal indicates
326 full supply nodes and points lying below the diagonal points denote partial supply against
327 design demand. It is found from PDA that network is able to supply 89.1 % of total demand



328 while supply from reservoir ID 272 is ceased. Out of 268 nodes, 90 nodes are able to make
329 partial supply to the consumers and remaining nodes could make the design supply. Fig. 7
330 presents the distribution of nodal pressure under no-component failure condition. The DDA
331 indicates that pressure at all the nodes is above H_{req} and hence full design supply is possible.
332 Fig. 8 indicates the distribution of nodal pressures when there is no supply from reservoir ID
333 272. The DDA shows the negative pressure at several nodes. From Fig.6 and Fig.9, it is
334 evident that proposed approach predicts nodal outflow corresponding to the pressure in all the
335 nodes above H_{min} .

336 Further, supply from reservoir ID 270 is closed and proposed approach is applied. It is
337 noticed that DDA has shown 232 nodes as pressure deficient nodes. In absence of supply
338 from reservoir ID 270, the network is able to supply 78.46% of total design demand. From
339 Fig 10, it is possible to notice that large number of supply nodes getting affected in absence
340 of Reservoir ID 270. 49% of total nodes could deliver full design supply and remaining could
341 make only partial supply. Table 8 presents the total outflow from the network obtained by
342 isolation of selected pipes. It is evident from results that the proposed approach is able to
343 find the nodal outflow under any pipe failure condition apart from pipe connecting the
344 source.

345 **6.0 Conclusion**

346 Pressure driven analysis (PDA) of water distribution network estimates realistic outflow at all
347 demand nodes while network is under pressure deficient conditions. Use of available network
348 components like reservoir, valves and emitter to simulate pressure based outflow is found to
349 be simple approach as it could be implemented easily for small networks without change of
350 source code of commercial software. But, the major bottleneck in adopting such an approach
351 is that large number of artificial components needs to be added to either all demand nodes or
352 deficient nodes. This increases the complexity of network configuration and also burden to



353 computation part. The proposed approach does not utilize the artificial components other than
354 emitter. Emitter is not a physical component to be added at the demand nodes. Instead it
355 requires an appropriate co-efficient to activate the emitter and estimate the outflow based on
356 available pressure at the node. By changing the nodal properties to those nodes categorized as
357 pressure deficit, the pressure based outflow is able to evaluate by proposed iterative approach
358 using emitter option alone. From the analysis of the results, it is evident that proposed
359 approach can be easily implemented for various pressure limits.

360

361 **Competing Interests**

362 The authors declare that they have no conflict of interest.

363

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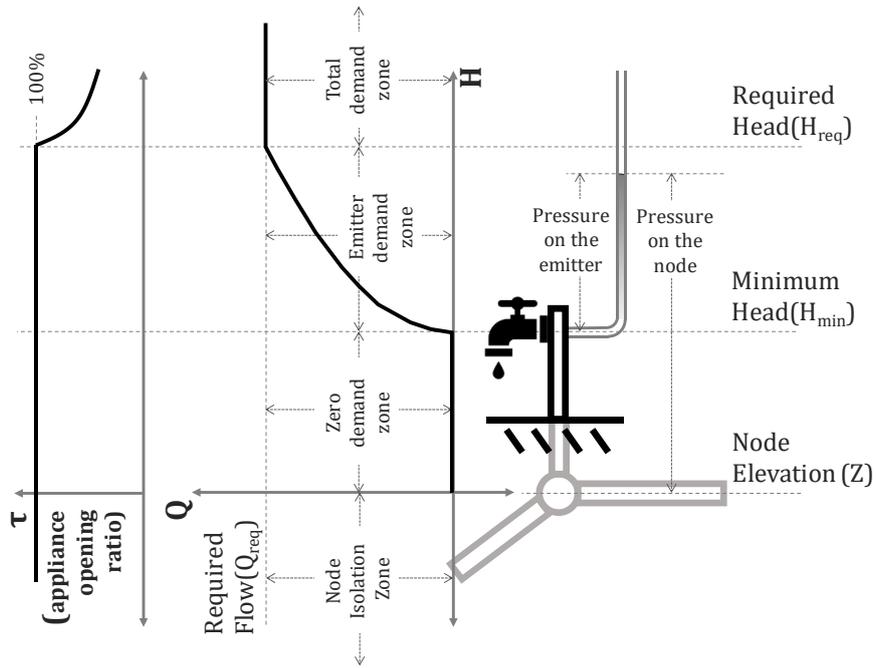
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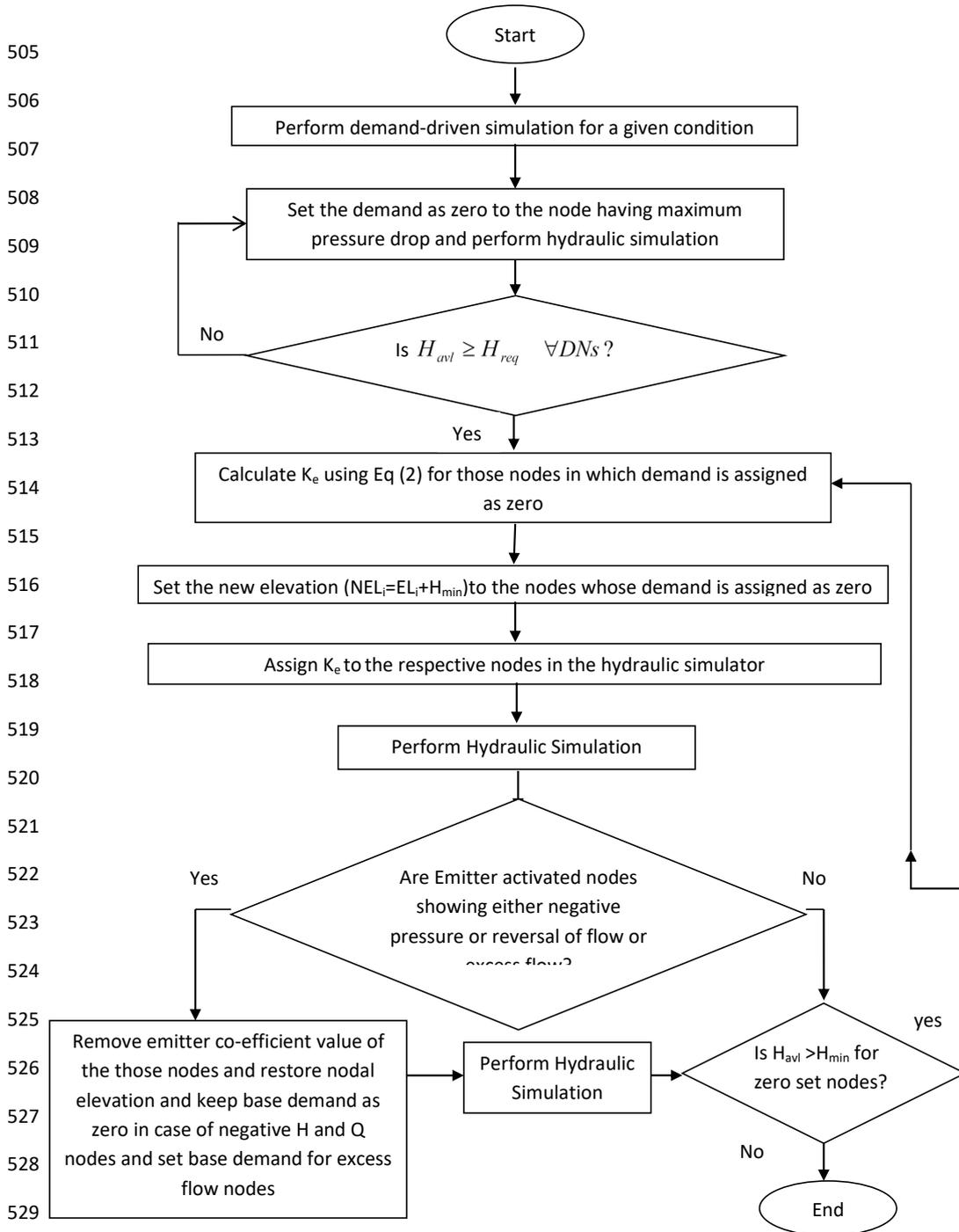


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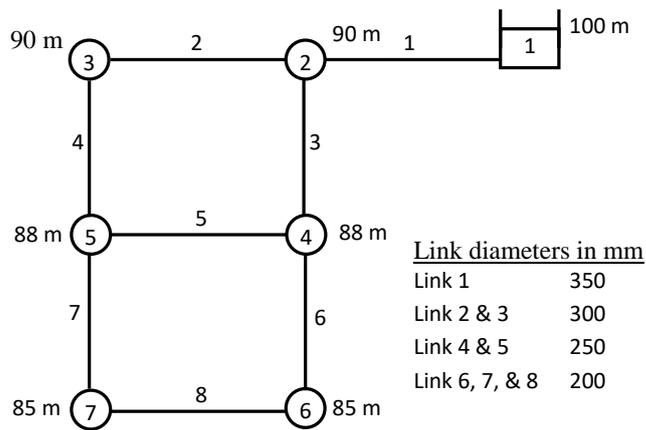
Fig.1 Interpretation of the nodal demand vs. head curve

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530 Fig. 2 Flow chart illustrate the computational steps involved in the proposed approach

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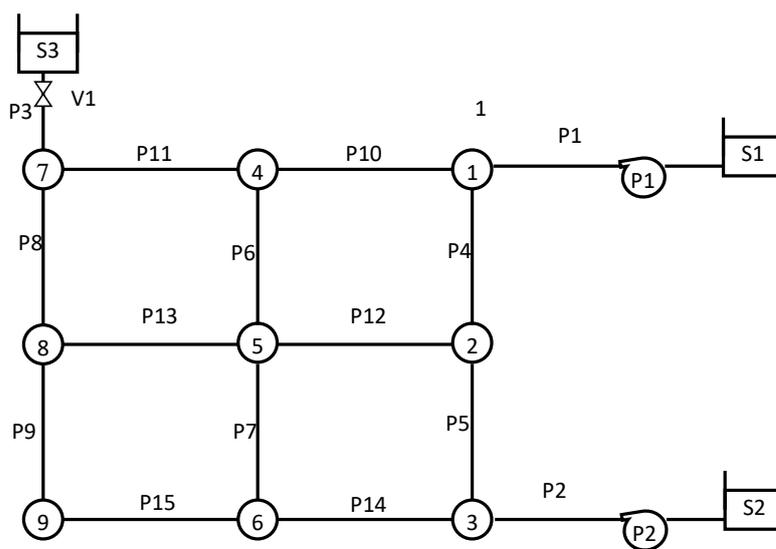
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Fig. 3 Layout of the Two-Loop network (Example 1 and 2)

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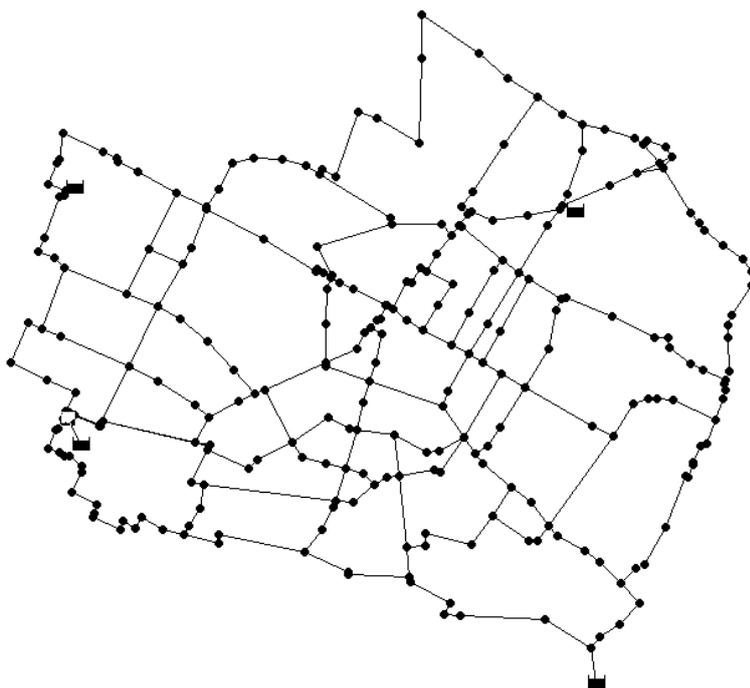


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Fig. 4 Layout of multisource pumped network (Example 3)

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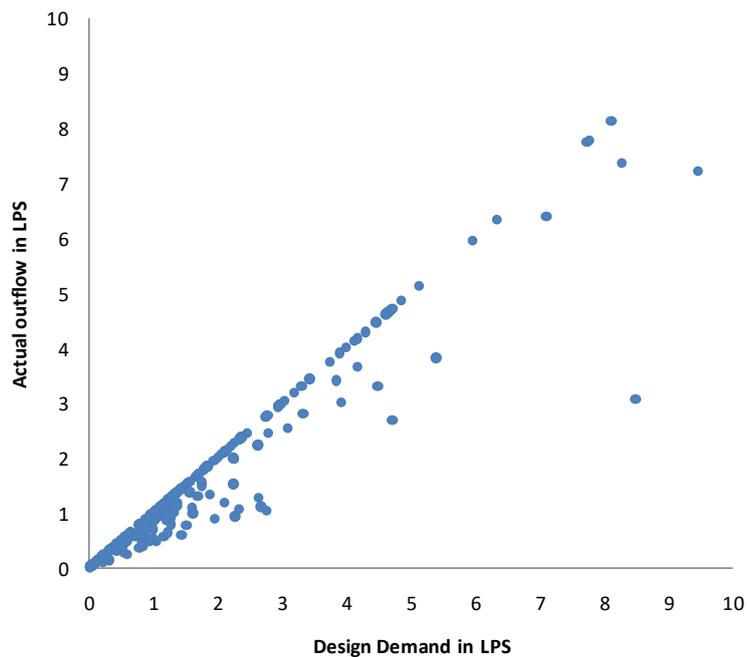
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Fig. 5 Layout of Modena Network (Example 4)

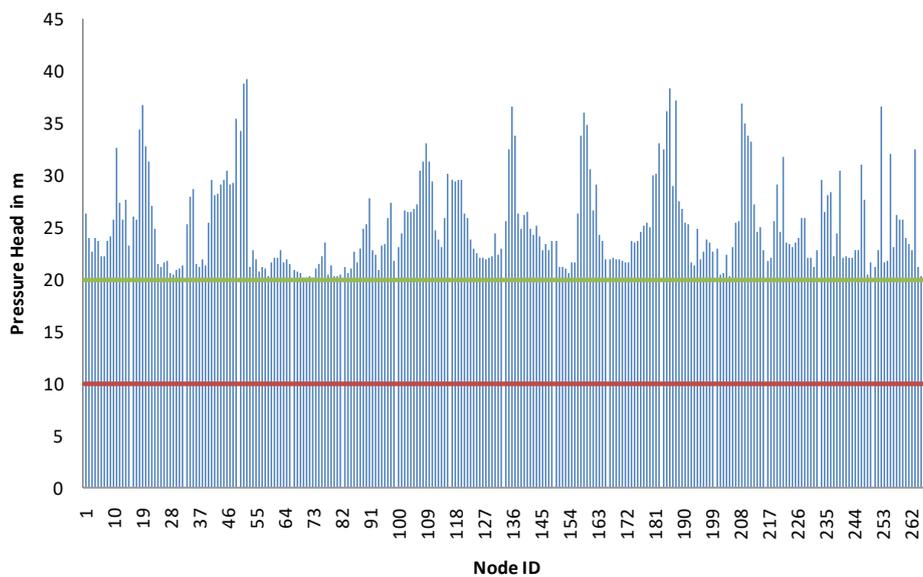


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Fig. 6 Actual outflow against design demand under no supply from Reservoir ID 272

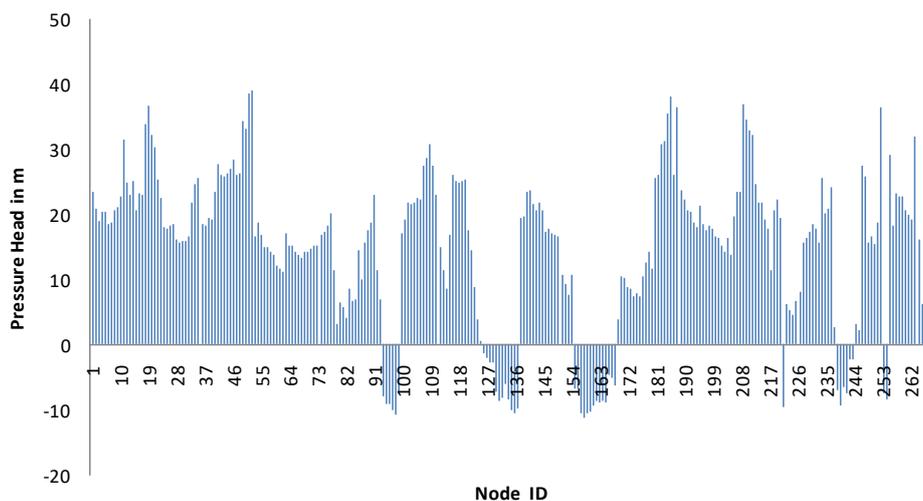
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Fig. 7 Nodal pressure head under no component failure condition

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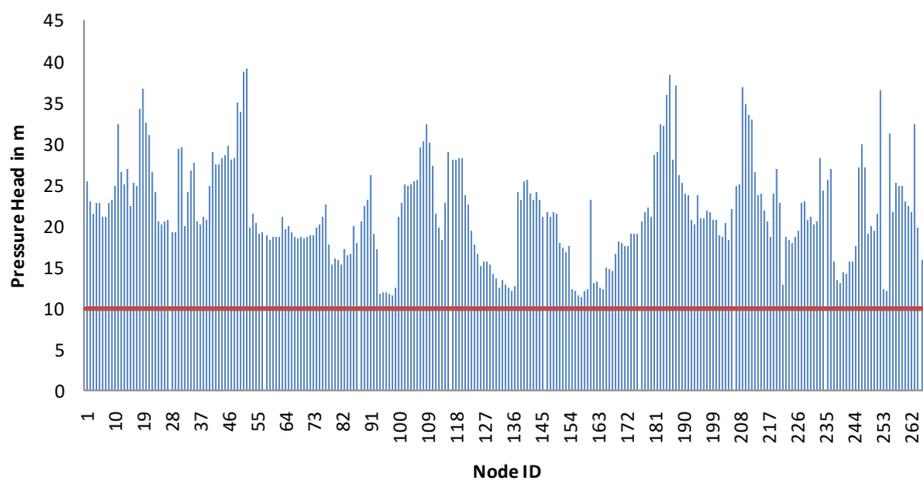


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Fig.8 Nodal pressure when Reservoir ID 272 disconnected (DDA)



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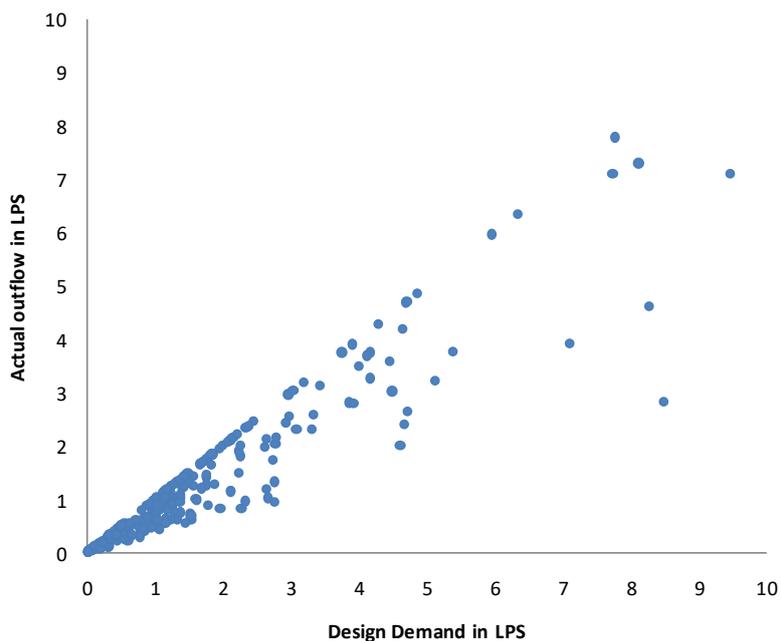
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Fig. 9 Nodal pressure when Reservoir ID 272 disconnected (PDA)

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Fig.10 Actual outflow against design demand when no supply from Reservoir ID 270

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Table 1 Various Head – Flow relationship for PDA

S.No	Author(s) & year	Year	Head-flow equation	Remark
1	Bhave	1981	$\left. \begin{aligned} q_j^{avl} &= q_j^{req} \text{ (adequate flow), if } H_j^{avl} \geq H_j^{min} \\ 0 < q_j^{avl} < q_j^{req} \text{ (partial flow), if } H_j^{min} = H_j^{avl} \\ q_j^{avl} &= 0 \text{ (no flow), if } H_j^{avl} \leq H_j^{min} \end{aligned} \right\}$	First attempt for pressure deficient analysis using simultaneous head-flow equations along with energy and mass balance equations.
2	Germanopoulos	1985	$q_j^{avl} = q_j^{req} (1 - 10^{-c_j (H_j^{avl} - H_j^{min}) / (H_j^{des} - H_j^{min})})$	C_j – node constant.
3	Wagner et al.	1988	$\left. \begin{aligned} q_j^{avl} &= q_j^{req}, \text{ if } H_j^{avl} \geq H_j^{min} \\ q_j^{avl} &= q_j^{req} \left(\frac{H_j^{avl} - H_j^{min}}{H_j^{des} - H_j^{min}} \right)^{1/n}, \text{ if } H_j^{min} < H_j^{avl} < H_j^{des} \\ q_j^{avl} &= 0, \text{ if } H_j^{avl} \leq H_j^{min} \end{aligned} \right\}$	n – Exponent constant (its value often taken as either 1.85 or 2).
4	Reddy and Elango	1989, 1991	$q_j^{avl} = S_j (H_j^{avl} - H_j^{min})^{0.5}$	S_j – node constant.
5	Chandapillai	1991	$H_j^{avl} = H_j^{min} + K_j (q_j^{avl})^n$	K_j - constant; n – exponent;
6	Fujiwara and Ganesharajah	1993	$\left. \begin{aligned} q_j^{avl} &= q_j^{req} \text{ for } H_j^{avl} \geq H_j^{des} \\ q_j^{avl} &= q_j^{req} \left(\frac{\int_{H_j^{min}}^{H_j^{avl}} (H_j^{avl} - H_j^{min})(H_j^{des} - H_j^{avl}) dH}{\int_{H_j^{min}}^{H_j^{avl}} (H_j^{avl} - H_j^{min})(H_j^{des} - H_j^{avl}) dH} \right), \text{ if } H_j^{min} < H_j^{avl} < H_j^{des} \\ q_j^{avl} &= 0 \text{ (no flow), if } H_j^{avl} \leq H_j^{min} \end{aligned} \right\}$	
7	Tucciarelli et al.	1999	$\left. \begin{aligned} q_j^{avl} &= q_j^{req}, \text{ if } H_j^{avl} \geq H_j^{min} \\ q_j^{avl} &= q_j^{req} \sin^2 \left(\frac{H_j^{avl}}{H_j^{min}} \right), \text{ if } 0 < H_j^{avl} < H_j^{min} \\ q_j^{avl} &= 0, \text{ if } H_j^{avl} \leq 0 \end{aligned} \right\}$	
8	Tanyimboh et al.	2001	Same as the equation of Wagner et al. (1988)	Drove Wagner's (1988) equation from Chandapillai (1991) equation. Using this attempted to find reliability of node as well as the network.
9	Wu et al.	2009	$\left. \begin{aligned} q_j^{avl} &= 0, \text{ if } H_j^{avl} \leq 0 \\ q_j^{avl} &= q_j^{req} \left(\frac{H_j^{avl}}{H_j^{des}} \right)^{1/n}, \text{ if } H_j^{avl} < H_j^{thr} \\ q_j^{avl} &= q_j^{req} \left(\frac{H_j^{thr}}{H_j^{des}} \right)^{1/n}, \text{ if } H_j^{avl} \geq H_j^{thr} \end{aligned} \right\}$	H_j^{thr} - threshold pressure above which the demand is independent of nodal pressure.
10	Tanyimboh and Templeman	2010	$q_j(H_j) = q_j^{req} \frac{\exp(\alpha_j + \beta_j H_j)}{1 + \exp(\alpha_j + \beta_j H_j)}$ $\alpha_j = \frac{-4.595 H_j^{des} - 6.907 H_j^{min}}{H_j^{des} - H_j^{min}}$ $\beta_j = \frac{11.502}{H_j^{des} - H_j^{min}}$	
11	Jun and Guoping	2013	Considered volume driven demand, pressure driven demand and leaks.	Modified EPANET for nodal outflows



				based on pressure-dependent demand formulations and leakage models (EPANET-MNO).
12	Morley and Tricarico	2014	Modified source code of EPANET by introducing emitters.	Each emitter is assigned with its own empirical exponent. Convergence issues when applied to complex or larger WDNs.

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Table 2 Use of artificial components in PDA

S.No.	Author(s) & year	Year	Component used in demand driven analysis	Remark
1	Ang and Jowitt	2006	Artificial reservoir and artificial pipe at each node	First (iterative) demand driven application for pressure deficient analysis. Popularly known as PDNA (Pressure-Deficient Network Algorithm)
2	Baek et al.	2010	Nil	Instead of iterative procedure, used an optimization model. DDA model and head-flow relationships were also used.
3	Suribabu and Neelakantan	2011	Artificial complementary reservoir and artificial pipe only at pressure deficient nodes	This approach used is known as CRS (Complementary Reservoirs Solution) method. <i>Second author is the PI of this proposal.</i>
4	Jinesh Babu and Mohan	2012	Artificial reservoirs, artificial flow control (to control flow to artificial reservoirs), check valves (to avoid negative pressure) and artificial pipe at pressure deficient nodes	Demonstrated limitation of the Ang and Jowitt (2006) method. Reduced the number of iterations required significantly. Popularly known as Modified PDNA (MPDNA).
5	Gorev and Kodzhespirova	2013	Artificial reservoirs, artificial flow control valves, artificial check valves and additional artificial pipes.	Results obtained in a single hydraulic run, Supports only parabolic type of node head-flow relationship.
6	Sivakumar and Prasad	2014	Artificial reservoirs, artificial flow control valves, artificial check valves and artificial pipe	Highlighted limitations of the Ang and Jowitt (2006) method. Reduced the number of iterations required significantly. Could not simulate partial flow between the minimum and the desired pressure head levels.
7	Abdy Sayyed et al.	2013, 2014, 2015	Replaced the artificial reservoir and artificial pipe with a flow emitter	Works excellent for steady-state analysis. Did not consider minimum pressure head level.
8	Sivakumar and Prasad	2015	Artificial reservoirs, artificial flow control valves, artificial check valves and additional artificial pipes.	Compared MPDNA with different head-flow relationships. Proposed modifications to MPDNA. No need for iterative procedures.
9	Suribabu	2015	Emitter	Compared Emitter based PDA with other PDA based on Head-Flow relations
10	Mamizadeh and Sharoonizadeh	2016	Among the two methods, in one method, the components added are same as in CRS approach of Suribabu and Neelakantan (2011). Added a flow control valve in another method.	Proposed two modified versions of CRS method (MCRS) to overcome certain drawbacks.
11	Sharoonizadeh and Mamizadeh	2016	Compared PDNA, MPDNA, CRS and MCRS methods.	Concluded that MPDNA and MCRS methods are better,
12	Suribabu et al.	2017	Artificial reservoirs and artificial pipes.	Improved CRS method proposed.
13	Mahmoud et al.	2017	Artificial check valve, artificial flow control valve, artificial flow emitter, dummy node and artificial pipes at each pressure deficient node	Single-iteration pressure driven analysis (SIPDA). Uses Wagner et al. (1988) node head-flow relationship.



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596 **Table 3 Step by step analysis results showing nodal outflows and pressure at each level**
597 **of simulation**

Demand (L/s) and Available pressure (m)						
Simulation	Node 2	Node 3	Node 4	Node 5	Node 6	Node 7
Pipe 3 closed condition						
1 (pipe 3 closed)	25.00 (3.57)	25.00 (-6.14)	25.00 (-23.17)	25.00 (-19.76)	25.00 (-22.31)	25.00 (-22.06)
2 (Zero demand to node 4)	25.00 (5.42)	25.00 (-1.01)	0.00 (-9.21)	25.00 (-8.18)	25.00 (-9.28)	25.00 (-9.25)
3 (Zero demand to node 6)	25.00 (6.97)	25.00 (3.20)	0.00 (0.66)	25.00 (0.87)	0.00 (3.05)	25.00 (2.43)
4 (Set K_e to node 4 and 6)	25.00 (6.82)	25.00 (2.80)	-18.34 (0.00)	25.00 (0.05)	20.94 (0.00)	25.00 (-0.03)
5 (Remove k_e at node 4 and close the pipes incident to the node)	25.00 (6.94)	25.00 (3.11)	Isolated	25.00 (0.70)	0.54 (0.00)	25.00 (0.00)
50 L/s Fire demand at node 2						
1 (Set demand at node 2 as 75 L/s)	75.00 (-0.95)	25.00 (-3.12)	25.00 (-2.21)	25.00 (-2.87)	25.00 (-3.09)	25.00 (-3.11)
2 (Set Zero demand at node 3)	75.00 (1.45)	0.00 (0.50)	25.00 (0.60)	25.00 (0.21)	25.00 (-0.15)	25.00 (-0.16)
3 (Set Zero demand to node 7)	75.00 (3.57)	0.00 (3.03)	25.00 (3.88)	25.00 (3.72)	25.00 (5.46)	0.00 (6.09)
4 (Change nodal property for nodes 3 and 7)	75.00 (1.16)	6.25 (0.00)	25.00 (0.38)	25.00 (-0.05)	25.00 (0.00)	21.96 (0.00)
5 (Change nodal property for node 5)	75.00 (1.17)	6.81 (0.00)	25.00 (0.41)	24.06 (0.00)	25.00 (0.00)	22.26 (0.00)
50 L/s Fire demand at node 7						
1 (Set demand at node 7 as 75 L/s)	25.00 (-0.95)	25.00 (-4.66)	25.00 (-5.45)	25.00 (-6.88)	25.00 (-14.46)	75.00 (-17.56)
2 (Set Zero demand at node 7)	25.00 (5.42)	25.00 (3.88)	25.00 (5.37)	25.00 (5.01)	25.00 (6.87)	0.00 (7.44)
3 (Change nodal property at node 7)	25.00 (3.18)	25.00 (0.87)	25.00 (1.64)	25.00 (0.93)	25.00 (0.10)	29.93 (0.00)

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600 **Table 4 Step by step analysis results showing nodal outflows under two pressures**

Demand (L/s) and available pressure (m)						
Simulation	Node 2	Node 3	Node 4	Node 5	Node 6	Node 7
Pipe 3 closed condition						
1 (pipe 3 closed)	25.00 (38.57)	25.00 (28.86)	25.00 (11.83)	25.00 (15.24)	25.00 (12.69)	25.00 (12.94)
2 (Zero demand to node 4)	25.00 (40.42)	25.00 (33.99)	0.00 (25.79)	25.00 (26.82)	25.00 (25.72)	25.00 (25.75)
3 (Zero demand to node 6)	25.00 (41.97)	25.00 (38.00)	0.00 (35.66)	25.00 (35.87)	0.00 (38.05)	25.00 (37.43)
4 (Change nodal property for nodes 4 and 6 assign $K_e = 5.8$)	25.00 (39.85)	25.00 (32.42)	15.75 (21.36)	25.00 (23.32)	17.39 (22.64)	25.00 (22.64)
5 (Change nodal property for nodes 5 and 7 assign $K_e = 5.8$)	25.00 (40.17)	25.00 (33.32)	18.14 (23.26)	20.47 (25.34)	19.88 (24.74)	20.04 (24.93)
SIPDA						
$C_d = 5.8$	25.00 (40.02)	25.00 (32.91)	17.22 (22.50)	25.00 (24.42)	19.15 (24.13)	19.29 (24.26)
Proposed approach for isolation of Link 3 and 6						
1 (pipe 3 and 6 isolated)	25.00 (38.57)	25.00 (28.86)	25.00 (14.04)	25.00 (15.24)	25.00 (1.86)	25.00 (5.41)
2 (Set demand at node 6 as zero)	25.00 (40.42)	25.00 (33.99)	25.00 (25.62)	25.00 (26.82)	0.00 (26.27)	25.00 (26.27)
3 (Set demand at node 7 as zero)	25.00 (41.97)	25.00 (38.20)	25.00 (34.67)	25.00 (35.87)	0.00 (38.87)	0.00 (38.87)
4 (Change nodal property at nodes 6 and 7 assign $K_e = 5.8$)	25.00 (39.99)	25.00 (32.89)	25.00 (23.02)	25.00 (24.22)	14.66 (20.57)	16.45 (21.89)
5 (Change nodal property at nodes 4 and 5 and assign $K_e = 5.8$)	25.00 (40.34)	25.00 (33.78)	20.66 (25.51)	21.54 (26.35)	15.99 (21.54)	17.94 (23.09)



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Table 5 Nodal and Pipe properties of multisource pumped network

Node ID	Elevation (m)	Demand (m ³ /hr)	Pipe No.	Length (m)	Diameter (mm)
1	165	100	1	1000	457.2
2	160	150	2	1000	508.0
3	155	120	3	500	355.6
4	150	120	4	1000	203.2
5	150	200	5	1000	203.2
6	155	100	6	1000	355.6
7	160	100	7	1000	152.4
8	160	330	8	1000	355.6
9	160	240	9	1000	254.0
			10	1000	355.6
			11	1000	152.4
			12	1000	152.4
			13	1000	152.4
			14	1000	406.4
			15	1000	406.4

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605 Table 6 Design demand during different time steps for multisource pumped network

Node ID	Demand in m ³ /hr			
	Time step	Time step	Time step	Time step 4
	1	2	3	
1	20	100	60	80
2	30	150	90	120
3	24	120	72	96
4	24	120	72	96
5	40	200	120	160
6	20	100	60	80
7	20	100	60	80
8	66	330	198	264
9	48	240	144	192

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609 Table 7 Nodal outflows under pump 1 failure condition for Multisource pumped network

Nodal outflow (m ³ /hr) and Available pressure (m)										
Time step	N 1	N 2	N 3	N 4	N 5	N 6	N 7	N 8	N 9	Total flow
1	4.26	18.17	20.78	24	40	17.26	12.79	41.82	30.38	209.46
	15.86	20.93	26.49	30.86	30.86	26.44	21.57	21.44	21.43	
2	33.82	99.66	120.00	40.84	68.17	100.00	91.07	266.61	192.22	1012.39
	17.01	22.04	31.33	17.02	17.04	30.27	27.62	25.11	24.94	
3	0.00	45.50	65.63	68.71	114.49	53.81	43.29	133.79	96.73	621.94
	13.79	19.24	27.64	28.76	28.75	27.26	23.20	22.26	22.18	
4	0.00	52.68	90.02	86.83	144.66	73.05	61.60	183.49	132.54	833.58
	12.51	18.27	28.32	27.46	27.45	27.67	24.24	22.65	22.52	

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612 Table 8 Total outflow from Modena network selected links isolation condition

Link ID	Pipe Diameter (mm)	Deficit nodes as per DDA	Total outflow LPS
11	100	1	406.9321
22	200	63	400.8348
50	150	26	404.3639
68	200	115	391.5420
100	150	57	390.9427
157	300	180	362.8878
158	300	182	361.7787
224	125	11	406.7551
242	125	14	405.1062
250	100	0	406.9399
291	350	245	277.6133
292	350	247	264.3850

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